Practice and Theory of Blendshape Facial Models

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Abstract
“Blendshapes”, a simple linear model of facial expression, is the prevalent approach to realistic facial animation. It has driven animated characters in Hollywood films, and is a standard feature of commercial animation packages. The blendshape approach originated in industry, and became a subject of academic research relatively recently. This survey describes the published state of the art in this area, covering both literature from the graphics research community, and developments published in industry forums. We show that, despite the simplicity of the blendshape approach, there remain open problems associated with this fundamental technique.

Introduction
The face has always held a particular interest for the computer graphics community: its complexity is a constant challenge to our increasing ability to model, render, and animate lifelike synthetic objects. A variety of approaches to facial animation have been pursued, including:

- parametric models [Par74, Par91], in which custom deformation algorithms defined specifically for the face are implemented,
- approaches using proprietary deformers of commercial packages, such as “cluster deformers” [Tic09],
- physically-based models, which approximate the mechanical properties of the face such as skin layers, muscles, fatty tissues, bones, etc. [TW91, SNF05],
- meshes driven by dense motion capture [EYE, GGW*98, BPL*03, Mov09, BHPS10, BHB*11],
- principal component analysis (PCA) models obtained from scans or motion capture [BV99, BBPV03],
- approaches based on spatial interpolation [BBA*07] or interpolation in an abstract “pose” or expression space [LCF00, BLB*08, LH09, RHKK11],
- “blendshape” models, which are referred to with several other names (refer to the Terminology section), and
- hybrid approaches [KMML10].

Figure 1: Blendshapes are an approximate semantic parameterization of facial expression. From left to right, a half smile, a smile, and a (non-smiling) open-mouth expression. While the smile and open-mouth expressions are most similar in terms of geometric distance, the smile is closer to the half-smile in parameter distance (distance=0.36) than it is to the open-mouth expression (distance=1.34). Please enlarge to see details.

See [OBP*12, DN07, PW08, NN99] for further overview of facial animation approaches.

Among these choices, blendshapes remain popular due to the combination of simplicity, expressiveness, and interpretabil-
ity. Blendshape facial animation is the predominant choice for realistic humanoid characters in the movie industry. The approach has been used for lead characters in movies such as *The Curious Case of Benjamin Button* [Flu11], *King Kong* [SG06], *The Lord of the Rings* [Sin03], *Final Fantasy: The Spirits Within*, and *Stuart Little*. Even when more sophisticated approaches to facial modeling are used, blendshapes are sometimes employed as a base layer over which nonlinear or physically based deformations are layered.

A blendshape model generates a facial pose as a linear combination of a number of facial expressions, the blendshape “targets”. Each target can be a complete facial expression, or a “delta” expression such as raising one of the eyebrows. The Facial Action Coding System [ER97] has been used to guide the construction of the target shapes [SG06, Hav06]. Many of the targets in this system approximate the linearized effect of individual facial muscles. By varying the weights of the linear combination, a range of facial expressions can be expressed with little computation. The set of shapes can be extended as desired to refine the range of expressions that the character can produce. In comparison with other representations, blendshapes have several advantages that together explain the popularity of this technique:

- The desired shape of the face can be directly specified, by sculpting the blendshape targets. Other approaches provide indirect control over shape.
- Blendshapes are a *semantic parameterization*: the weights have intuitive meaning for the animator as the strength or influence of the various facial expressions (Figure 1). Other linear models such as PCA do not provide this (section 7.7).
- To some extent blendshapes force the animator to stay “on model”, that is, arbitrary deformations are not possible (Figure 2). While this could be seen as limiting the artist’s power, it helps ensure that the facial character is consistent even if animated by different individuals. It also enforces a division of responsibility between the character modeler and animator.

Although the blendshape technique is conceptually simple, developing a blendshape face model is a large and labor intensive effort at present. To express a complete range of realistic expressions, digital modelers often have to create large libraries of blendshape targets. For example the character of Gollum in the *Lord of the Rings* had 675 targets [For03, Sin03]. Generating a reasonably detailed model can be as much as a year of work for a skilled modeler, involving many iterations of refinement.

The remainder of this survey is organized as follows. The first three sections define our subject, while subsequent sections describe particular topics and summarize associated research and open problems. Section 1 collects the industry terminology of blendshapes. Section 2 presents a brief history, though most related literature will be discussed in relevant later sections. Section 3 describes blendshapes from a linear algebra point of view, including recent variants such as “combination” blendshapes. Section 4 surveys methods of constructing blendshape models, including model transfer and refinement of models. Section 5 reviews interaction and animation techniques including performance-driven and direct manipulation approaches. Section 6 considers blendshapes as a high-dimensional interpolation problem. Section 7 considers blendshapes as a parameterization, and contrasts this approach with those based on principal component analysis. Section 8 mentions several extensions of the blendshape idea.

1. Terminology

The “blendshapes” term was introduced in the computer graphics industry, and we follow that definition: blendshapes are linear facial models in which the individual basis vectors represent individual facial expressions. As a consequence the basis is not orthogonal in general. The individual basis vectors have been referred to as blendshape targets and morph targets, or (confusingly) as shapes or blendshapes. The corresponding weights are often called sliders, since this is how they appear in the user interface (Figure 3). A morphable model [BV09] is also a linear facial model, though it may focus on identity rather than expression, and its underlying basis is orthogonal rather than semantic.

From an artist’s point of view, the interpretability of the blendshape basis is a defining feature. To manage the scope of this survey we will not attempt to fully survey techniques that make use of an orthogonal basis. Since the distinction is less important from a mathematical and programming point of view, however, relevant concepts that have to date only been employed with orthogonal models will be mentioned.
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2. History

The origin of the blendshape approach is not generally associated with an academic publication, though it was well known in the computer graphics industry by the 1980s. Although Fred Parke is known for his pioneering work on the alternate parametric approach to facial modeling [Par72, Par74], he experimented with linear blending between whole face shapes [Par]. By the late 1980s the “delta” or offset blendshape scheme became popular [Bei05] and appeared in commercial software [Ber87, Els90]. In this variant a neutral face shape is designated and the remaining shapes are replaced by the differences between those shapes and the neutral shape. This results in localized control when the differences between the target shape and the neutral face are restricted to a small region, although it relies on the modeller to produce shapes with this property.

This idea was extended to a segmented face where separate regions are blended independently [Kle89], thus guaranteeing local control. A standard example is the segmentation of a face into an upper region and a lower region: the upper region is used for expressing emotions, while the lower region expresses speech [DBLN06].

While blendshape targets are most often considered as time-independent facial expressions, it is also possible to view individual blendshapes as being situated at particular times in the animation, and to simply cross-fade between them to produce the final animation. This time-dependent blendshape approach provides the most direct control possible by guaranteeing that desired expressions appear at particular points in the animation, but it requires the construction of many blendshapes that may not be reusable at other points in the animation. Some animations have combined the time-dependent and time-independent blendshape approaches [Zha01].

Additional literature on blendshapes will be mentioned in appropriate sections of the remainder of the survey.

3. Algebra and Algorithms

Some insight and ease of discussion can be had by viewing blendshapes as a simple vector sum. To be concrete, consider a facial model composed of \( n = 100 \) blendshapes, each having \( p = 10000 \) control vertices (“points”), with each vertex...
having three components $x,y,z$. By “unrolling” the numbers composing each blendshape into a long vector $b_k$ in some order that is arbitrary (such as $xxyyyyyyz$, or alternately $xyxzyzxyz$) but consistent across the individual blendshapes (Figure 4), the blendshape model is expressed as

$$ f = \sum_{k=0}^{n} w_k b_k $$

or using matrix notation

$$ f = Bw $$

where $f$ is the resulting face, in the form of a $m = 30000 \times 1$ vector ($m = 3p$), $B$ is a $30000 \times 100$ matrix whose column vectors, $b_k$, are the individual blendshapes ($30000 \times 1$ vectors), and $w$ are the weights (a $100 \times 1$ vector). We take $b_0$ to be the blendshape target representing the neutral face. This linear algebra viewpoint will be used to describe various issues and algorithms.

Equation (2) represents the global or “whole-face” blendshape approach. In this approach scaling all the weights by a multiplier causes the whole head to scale. Overall scaling of the head is more conveniently handled with a separate transformation, however. To eliminate undesired scaling the weights in equation (2) may be constrained to sum to one. Additionally the weights can be further constrained to the interval $[0,1]$, as described in section 7.5.

3.1. Delta blendshape formulation

In the “delta” blend shape formulation, one face model $b_0$ (typically the resting face expression) is designated as the “neutral” face shape, and the remaining targets $b_k$, $k = 1 \ldots n$ are replaced with the difference $b_k - b_0$ between the $k$th face target and the neutral face:

$$ f = b_0 + \sum_{k=1}^{n} w_k (b_k - b_0) $$

(with $b_0$ being the neutral shape). We denote this as

$$ f = b_0 + Bw $$

(note that we are reusing variable names from equation (2)). In this formulation the weights are conventionally limited to the range $[0,1]$, although there are exceptions to this convention. For example the Maya [Tic09] blendshape interface allows the $[0,1]$ limits to be overridden by the artist if needed.

If the difference between a particular blend shape $b_k$ and the neutral shape is confined to a small region, such as the left eyebrow, then the resulting parameterization offers intuitive localized control.

The delta blendshape formulation is used in popular packages such as Maya, and our discussion will assume this variant if not otherwise stated. Many comments apply equally (or with straightforward conversion) to the whole-face variant.

A blendshape model can be considered as placing targets at some of the vertices of a $n$-dimensional hypercube, with the origin being the neutral shape, and hypercube edges representing weights on the corresponding targets (Figure 5). Note that this and following figure are schematic, with a small face image representing the collection of vertex components of a particular blendshape target.

3.2. Intermediate shapes

As an individual weight in Eq. (4) varies from zero to one, the moving vertices on the face travel along a line. To allow more fidelity, production blendshape implementations such...
as that in Maya [Tic09] allow targets to be situated at intermediate weight values, giving piecewise linear interpolation. This is shown schematically in Figure 6.

3.3. Combination blendshapes

Another blendshape variant [Osi07, Ver, ZO14] adds additional “correction” shapes that become active to the extent that particular pairs (or triples, etc.) of weights are active. This scheme is variously called combination blendshapes or corrective shapes [ZO14].

This approach might be notated as

\[ f = f_0 + w_1 b_1 + w_2 b_2 + w_3 b_3 + \cdots + w_1 w_5 b_{1,5} + w_2 w_3 b_{2,3,10} + \cdots \]

Here the first line is equivalent to equation (4). A term \( w_1 w_5 b_{1,5} \) is a bilinear “correction” shape that is fully added only when \( w_1 \) and \( w_5 \) are both one, and is completely off if either is zero. The irregular numbering 1, 5 is intended to indicate that these corrections are only needed for particular pairs (or triples, quadruples) of shapes such as shape 1 and shape 5. For example, the eyebrow and mouth corner are spatially well separated, so it is unlikely that any correction shape would be needed for this pair of shapes. A schematic visual representation of this approach is shown in Figure 7. The combination targets are situated at (some of) the diagonals of the blendshape hypercube.

The majority of the blendshape targets in modern professional models with hundreds of targets are these combination shapes. As an example, the primary targets (those situated at the hypercube vertices that are neighbors of the neutral shape) may number 100 shapes, whereas the number of combination shapes may be several hundred or more [Rai04]. The combination blendshape idea should be distinguished from the on-line “correction” shapes that have been a subject of recent research (section 4.3). Correction shapes modify or add to the linear blendshape basis, whereas combination shapes can be seen as a second-order term in a Taylor series in the blendshape weights (section 6.4).

The combination blendshape scheme is not ideal from an interpolation point of view. When the facial expression travels along the (hyper)diagonal toward a 2nd order correction, the correction appears quadratically as \( w_i w_j b_{i, j} \). Subjectively, this means that the correction has little effect over most of the range of the sliders and then appears relatively suddenly. The problem is exacerbated with 3rd and higher order corrections. This problem can be partially addressed by placing intermediate shapes along the diagonal.

3.4. Hybrid rigs

In a blendshape model the jaw and neck are sometimes handled by alternate approaches. For example, since the motion of the jaw has a clear rotational component, the jaw-open target is often augmented by linear blend skinning [OBP*12]. The eyelids are another area that is sometimes handled by alternate rigging approaches, again due to the rotational motion. Refer to [OBP*12] for a recent survey of facial rigging techniques.

4. Constructing Blendshapes

There are several approaches for creating blendshapes. A skilled digital artist can deform a base mesh into the different shapes needed to cover the desired range of expressions. Alternatively, the blend shapes can be directly scanned from a real actor or a sculpted model. A single template model can be registered to each scan in order to obtain vertex-wise correspondences across the blendshape targets. Methods to register scans (and register a generic template to scans) include [LDSS99, ARV07, SE09, WAT*11, ACP03, ASK*05].
In concept, a dynamic mesh obtained from dense motion capture can be decomposed into a linear model using principal component analysis (PCA) or other approaches. However, the PCA models lack the interpretability of blendshapes. This will be discussed further in sections 4.2 and 7.7.

In [PHL'98] blendshape targets are rapidly constructed with minimal manual assistance from multiple pictures of an actor. [BV99] fits a morphable model (PCA model of both the geometry and texture) to a single image, resulting in an estimate of the geometry and texture of the person’s face. Typically the geometry of a facial model is fairly coarse, with fine scale details such as wrinkles and freckles represented via textures, bump or normal maps, or recent techniques such as [MJC'08, BLB'08, BBB'14]. In the case of bump or normal maps the decomposition makes good use of graphics hardware, and the choice of relatively coarse geometry in facial model capture and tracking applications can also be motivated from bias-variance considerations in model fitting [HTF09].

4.1. Model transfer

Blendshape models can also be constructed by transferring the expressions from an existing source model to a target model with different proportions. Section 5.3 describes “expression cloning” algorithms for transferring the motion from one model to another. This subsection describes the related problem of constructing a target expression such as the neutral face. We term this problem model transfer. Note that model transfer algorithms can be used for transferring motion as well, simply by applying them to a moving source model. However not all expression cloning algorithms are suitable for model transfer.

Deformation transfer [SP04] is the leading approach for constructing a target model by model transfer. It requires a fully constructed blendshape model for the source, but only a neutral model for the target. This approach first finds the deformation gradient between each triangle of the neutral pose source model \( b_0 \) and the corresponding triangle in one of the source blendshape expressions \( b_k, k \geq 1 \) (The “deformation gradient” is the Jacobian of the function that deforms the source triangle from its neutral position). Then, given a non-neutral expression on the source model, deformation transfer finds triangles on a target expression so that the target deformation gradient matches the equivalent Jacobian on the source model in a least squares sense. [BSPG06] points out that deformation transfer is a form of Poisson equation.

Since the original deformation transfer does not consider collisions, it may result in self-collisions particularly around the eyelids and lips. [Sai13] inserted virtual triangles into the eye and mouth openings of the mesh to prevent this problem. They also add a new term to the optimization that causes the Laplacian of target mesh to resemble that of the source in areas that are most compressed or stretched, reducing a tendency to crumple in these areas.

[LWP10] is a technique designed specifically for the blendshape model transfer problem. This approach allows the artist to guide the model transfer process by specifying a small number of example expressions and corresponding approximate expected blendshape weights for these expressions. Since only a small number of example expressions are provided, construction of the full target basis is an underdetermined problem. This is solved by using the deformation transfer of the source as a regularization energy in their optimization.

4.2. Discovery of blendshapes

Creating a realistic blendshape model may require sculpting on the order of 100 blendshape targets, and many more shapes if the combination shapes scheme is used (section 3.3). Each target must be designed to capture its intended role such as approximating the activation of a particular muscle, while simultaneously minimizing undesirable interactions with other shapes. This is a labor intensive and iterative effort.

It would be ideal if one could start with dense motion capture of a sufficiently varied performance, and then automatically or semi-automatically convert this into a blendshape model. In abstract this is a matrix factorization problem

\[
M \approx BW
\]

where for a motion capture performance with \( t \) frames and \( p = m/3 \) vertices, the \( m \times t \) performance matrix \( M \) is split into the \( m \times n \) blendshape basis \( B \) and the \( n \times t \) animation weights matrix \( W \). Typically the number of frames \( t \) is larger than the number of basis vectors \( n \), so this is a low-rank factorization. Doing PCA on the dense motion capture might be a first step toward this goal, however as pointed out elsewhere, the PCA basis vectors are global and lack the necessary semantics. Given a PCA model \( f = Uc + m \) with \( U \) being the eigenvectors and \( m \) the mean shape, the discovery problem can be formulated as finding a “recombination” matrix \( R \) such that the new basis \( UR \) in an equivalent model

\[
f = (UR)(R^{-1}c) + n
\]

is more sparse [LMN04].

[NVW'13] addresses this blendshape discovery problem by minimizing \( \|M - BW\|_2^2 \) subject to a sparsity penalty on the basis \( B \), where \( M \) is the sequence of scans or motion capture of the face, and \( W \) are the corresponding (unknown) weights. Rather than minimizing \( \|B\|_1 \) to promote sparsity, they use an \( \ell_1 \) norm over the length (\( \ell_2 \) norm) of each vertex. In other words, each vertex in the basis is encouraged to be zero, but if the vertex is not zero then there is no further
penalization of its components [BJMO12]. The results out-
perform PCA, ICA, and several other algorithms and allow
intuitive direct manipulation editing.

While [NVW+13] is a significant advance, further develop-
ments may be possible on this important problem. It is likely
that artists will prefer to guide the blendshape construction
rather than relying on a fully automatic process, so an ideal
solution must accelerate the artist’s process without taking
away control.

4.3. Blendshape refinement

Often a blendshape model will not exactly match the de-
sired motion. One variant of this problem is when the motion
causes the model to take on an expression that reveals unde-
sirable interactions between the blendshape targets. In this
case artists can resculpt the model or add corrective combi-
nation shapes as discussed in section 3.3. A second form of
the problem is when the model matches the motion in a least
squares sense but with a large residual.

To handle this case [JTDP03] fit the residual with a radial
basis function scattered interpolation. [CLK01a] used a co-
ordinate descent optimization to solve for positions of the
basis vertices corresponding to the markers. This correction
was then applied to the remaining vertices using radial basis
interpolation. [KSSN11] addresses the refinement problem
by augmenting the basis with new targets for frames with
high residuals. The correction uses biharmonic interpo-
lation [BBA+07] of the tracked displacements.

While some of the previous methods optimize over all
frames in a sequence, a focus of recent research is methods
that can accomplish on-line refinement of the blendshape ba-
sis. Since the data in online methods is often of low quality,
a key issue is to distinguish geometry from noise, and to
decide when to stop adapting the basis. [LYYB13] address
this problem using a color-depth video stream. The initial
blendshapes of the actor’s face are created using deforma-
tion transfer. Then, additional corrective PCA shapes refine
the actor-specific expressions on the fly using incremental
PCA based learning. [BGY+13] presents a system to refine
animation curves and produce additional correctives from a
set of blendshapes along with 2D features such as markers on
the face and contours around eyelids and lips. Every frame
is optimized using 2D marker constraints, 3D bundle con-
straints, and contour constraints. [BWP13] combine a PCA
model of identity with a blendshape model of expressions
obtained through deformation transfer from a generic tem-
plate model. Since a particular person’s expressions are not
exactly captured in this basis, they add a correction in the
form of the low-frequency eigenvectors of the graph Lapla-
cian of the face mesh. This correction basis can fit a smooth
residual from the blendshape basis while rejecting the noise
from the RGB-D camera used in their system.

4.4. Detail enhancement

An existing prior database of high-resolution facial poses

4.5. Generating new models by interpolating in an
existing population

We informally refer to the set of mesh vertices and edges
as a topology. Given an existing set of blendshape models

4.6. Compressing blendshapes

While the blendshape representation provides compression
of an animation, further compression is desirable for ani-
mation editing, and is required for games. As an example
for discussion, a blendshape model with 10000 targets, each
with 10000 vertices represented with four-byte floats, would
require 120 megabytes of memory. In the delta blendshape
form most targets are localized and are zero at most vertices,
so this size can be reduced using a suitable sparse matrix
data structure.

While these figures indicate that a reasonably detailed model
is easily accommodated in the memory of current processors, there are two reasons for needing additional compression. First, it is desirable (and required in games) that the scene includes the character body and background complete with textures. As well, many scenes have multiple characters. A more important reason is that the matrix-vector multiply $Bw$ in equation (2) is memory-bound on both current CPUs and GPUs.

The obvious approach to compressing a blendshape model is to apply principal component analysis, retaining only the eigenvectors corresponding to the largest eigenvalues. As a rule of thumb, PCA can provide 10:1 or greater compression of many natural signals with little visible change in the signal. PCA does not work as well for blendshape models, however, because blendshapes are already a compressed representation—an animation of any length requires storage of only the $n$ basis vectors, and $n$ weights per frame. In several tests on available models, [SILN11] found that the compression rates obtainable using PCA without introducing visible degradation are as small as 3:1. Another issue that is frequently overlooked is that the PCA coefficients are dense (Figure 15), which may result in reduced performance relative to blendshapes!

While blendshape models are resistant to PCA compression, they nevertheless have considerable structure and smoothness that can be exploited. [SILN11] observe that it is possible to re-order the blendshape matrix $B$ to expose large low-rank blocks. Placing these in “off diagonal” positions allows application of hierarchically semi-separable (HSS) algorithms [XCGL10]. These approaches produce a hierarchical compressed representation by compressing off-diagonal blocks and then recursively processing the diagonal blocks, and they provide a fast and parallelizable matrix-vector multiplication. Using a HSS representation [SILN11] obtained on the order of 10:1 compression and similar speed increases.

4.7. Summary

Approaches to constructing blendshapes have developed considerably in the last decade, including custom algorithms for face capture [BBB'10], the introduction of model transfer algorithms, algorithms for localized basis discovery, and tracking algorithms that provide on-line refinement of the blendshape basis. The current state of the art should easily permit automated capture of a blendshape-like facial basis suitable for automated tracking. There may be room for future methods that incorporate human guidance in the construction process and provide a basis that is closer to the muscle- or expression-based blendshape bases described in industry forums [Osi07, fxg11, Hav06].

5. Animation and Interaction Techniques

Animating with blendshape requires specifying weights for each frame in the animation. For our discussion, animation techniques will be broadly divided into performance-driven animation techniques, keyframe animation, and direct manipulation. Performance-driven animation is commonly used to animate characters different from the actor, so expression cloning techniques will also be surveyed here. The section will conclude with a brief survey of alternative editing techniques.

5.1. Keyframe animation

Blendshape models have traditionally been animated using keyframe animation of the weights (sliders). Commercial packages such as Maya provide spline interpolation of the weights and allow the tangents to be set at keyframes. As an approximate figure, professional animation requires a keyframe roughly every three frames. Many animators prefer that keyframes include keys for all targets, rather than putting keys on each curve independently.

5.2. Performance-driven animation

In performance-driven facial animation, the motion of a human actor is used to drive the face model [Wil90, TW91, CDB02, BBPV03, PL06, PL05, WLGP09, GVWT13]. Whereas keyframe animation is commonly used in animated films with stylized characters, performance-driven animation is commonly used for visual-effects movies in which the computer graphics characters interact with filmed characters and backgrounds. Because blendshapes are the common choice for realistic facial models, blendshapes and performance-driven animation are frequently used together.

The general literature on face tracking in general spans several decades and a complete survey is beyond the scope of this report. We will concentrate on performance capture methods that drive a blendshape rig. Techniques that drive a low-level representation such as a mesh will not be surveyed [Wil90, GGW ‘98, WFKvdM97, BPL’03, BHPS10, FHW’11, BHB’11]. Methods that involve a nonlinear or physical underlying model are also not considered [TW91, DM96, SNF05].

Performance capture methods might be classified into those that use 3D motion capture information as input [CLK01a, DCFN06] versus methods that do model-based tracking of video [PSS99, BBPV03, CXH03, RHKK11, BGY’13, CWLZ13, CHZ14]. Another distinction is whether a PCA basis [BBPV03] or blendshape basis [PSS99, CK01, CLK01a, CDB02] is used. [DCFN06] uses a PCA basis for the motion capture which is then retargeted to a blendshape basis through a nonlinear radial basis mapping. [TDITM11] uses overlapping local PCA models.
Model-based tracking of blendshapes solves for the blendshape weights at each frame so as to match a reference video. Recent research has achieved high quality tracking from monocular video [GVWT13]. Typically the weights are constrained to the range 0..1. When the source motion to match is available in the form of 3D motion capture, this is a constrained linear problem that can be solved with quadratic programming [CK01, CLK01a, JTD03]. When model-based tracking is used to match images from a video, the perspective nonlinearity requires the use of nonlinear optimization (unless weak perspective is employed). [PSS99] allowed soft constraints with a Levenberg-Marquardt algorithm.

With the popularity and affordability of low-cost commercial depth cameras (e.g., Microsoft’s Kinect), researchers have developed a number of techniques to utilize such cameras for performance driven facial animation. One approach does real-time tracking and transfers the facial movement to a user-specific blendshape face model that is manually constructed at the offline stage [WBLP11]. Recent advances include online modeling of user-specific blendshape faces (without the offline step) and introduction of adaptive corrective shapes at runtime for high-fidelity performance driven facial animation applications [BGY13, LYYB13, BWP13]. These basis refinement approaches are briefly surveyed in section 4.3.

5.3. Expression cloning

In expression cloning techniques [NN01, SP04], the motion from one facial model (the “source”) is retargeted to drive a face (the “target”) with significantly different proportions. Expression cloning is frequently the goal of performance-driven animation. For example, an adult actor may produce the motion for a younger or older person (as in the movies The Polar Express and The Curious Case of Benjamin Button) or a non-human creature (as in Avatar and the Gollum character in the Lord of the Rings movies). A very similar problem is that of creating a full target face model, given the source face but only limited samples of the target, usually only the neutral shape. This problem discussed in section 4.1. Algorithms such as [SP04] mentioned in that section can also be used for expression cloning. [NN01] introduced the expression cloning problem. Their approach requires only a generic animated facial mesh for the source and makes no assumption of a blendshape or other representation. It establishes a mapping by finding corresponding pairs of points on the source and target models using face-specific heuristics. [VBPP05, DSJ11] discover a tensor basis that spans both expression and identity in different dimensions. Identity can be flexibly manipulated in this approach, however it does not use a blendshape basis.

A common approach to expression cloning is what might be termed “corresponding parameterization” [CLK01b, HIWZ05, PL06, LWP10]: source and target blendshape models are constructed to have the same number of targets, with the same semantic function (typically FACS inspired). The blendshape weights are then simply copied from source to target. This approach is simple, and allows great flexibility in developing the cross-mapping. For example, one could imagine a smile blendshape for a lizard character in which the mouth corners move backward whereas in the corresponding blendshape for the human the mouth corners are displaced upward. Expression cloning using corresponding parameterization based on FACS expressions [ER97] was introduced in the movie industry on projects such as Monster House and King Kong [fxg11].

The corresponding parameterization approach requires artists to construct blendshape models for both the source and target faces. In the usual case where the source is obtained by performance-driven animation, this can be avoided by requiring the actor to produce the set of basis expressions, for example by mimicking FACS expressions. Producing expressions consisting of individual facial muscles is an unnatural and difficult task for many people, however. In fact it is believed that some facial muscles can only be activated indi¬rectly, as a side effect of producing other expressions, but not under voluntary control [Ekm90].

Alternately, the source basis can be obtained by taking expressions from an actual performance. Chuang and Bregler [CB02] experimented with several principles for choosing frames from the performance, finding that the best approach selects expressions that have maximal projection on the leading principal components of the source performance. Specifically, the first two basis shapes are those that have the largest and smallest projection on the leading eigenvector, the second two have the maximum and minimum coefficients on the second axis, and so on. The artist then poses the target model to correspond to each of the chosen basis vectors. Note that while this algorithm involves PCA, the actual basis shapes are not expressions from the performance rather than eigenvectors, so creating a corresponding pose on the target model is a natural task. [CB02] also found that requiring the weights to be positive produced better cloning than allowing negative weights, even though the resulting reconstruction of the source animation has higher error. Intuitively, allowing negative weights allows the basis to “explain” small details of the source motion using a variety of unintended cancelling (positive and negative) combinations of the basis shapes, which has poor results when the same weights are applied on the target model. This intuition is related to the interpretation of non-negative matrix factorization as a parts-based decomposition [LS99].

More generally, if the source and target models already exist, but do not share a parameterization, it may be possible to learn a cloning function given sufficient examples of corresponding poses. In a linear version of this idea, there need to be \( c \geq n \) corresponding poses if the models contain \( n \)}
blendshape targets. Let \( w_k \) be the blendshape weights for the source, and \( v_k \) be the blendshape weights for the target, for each pair \( k \) of corresponding poses. Gather \( w_k \) and \( v_k \) as the columns of matrices \( W, V \) of dimension \( n \times c \). Then an expression cloning matrix \( E \) of dimension \( n \times n \) that maps \( w \) to \( v \) can be found,

\[
W = EV \\
WV^T = EVV^T \\
E = WV^T (VV^T)^{-1}
\]

This simple linear expression cloning approach has its limitations – in particular in that the mapping is linear (as is the case with some other approaches including corresponding parameterization).

Still more generally, in what might be termed semantic correspondence the source and target representations need only agree on a set of parameters that control the expression, with each having some mapping or algorithm to convert between these parameters and the internal representation of the model. This general approach may have been first demonstrated by SimGraphics in the 1990s [Wil01].

Most existing expression cloning algorithms do not consider adapting the temporal dynamics of the motion to the target character, and instead assume that if each individual frame can be transferred correctly, the resulting motion will be correct. This will tend to be the case if the source and target are of similar proportions.

There are several scenarios in which the temporal dynamics of face movement should be considered however. One case is where the target cannot reproduce the full range of movement of the source model. For example, the target jaw may not open widely enough to reproduce the source motion. These limits commonly occur when a blendshape model is driven directly by motion capture. They also can occur even when the source is a blendshape model. For example, the target model might allow jaw-open to range up to 1, but it may be that the results look unnatural if smile is simultaneously active with a value of more than 0.7. This situation can be crudely handled with an expression that sets the limit on the jaw-open as

\[
jaw-open-limit = 1 - 0.3 \times \text{smile}.
\]

In this situation, [SLS’12] argue that reproducing the source on a per-frame basis results in unnatural motion when the target motion limit is reached and exceeded. They propose that it is better to preserve the overall shape of the motion, rather than matching the position of each frame independently. This objective is by saying that the temporal derivatives (rather than positions) should be matched in a least squares sense. This leads to a space-time Poisson equation that is solved for the target blendshape motion.

More generally, most current expression cloning techniques require that the target expression for a particular frame be a function of the source expression for that frame only. More powerful expression cloning techniques may require looking at adjacent frames in order to allow anticipation and coarticulation-like effects to be produced.

An open problem is the case in which the target motion should differ from that of the source is when the target has significantly different proportions or size from the source. The human mouth moves very quickly during speech – for example the mouth can change from a fully open to a fully closed position in two adjacent video frames. Transferring this rapid motion to a large and non-humanoid character such as a whale would likely give implausible looking results.

On the other hand, we recall the anthropomorphic principal that the target character is usually humanoid if not human – if the character needs to be perceived by human audiences, it needs to express facial emotion in human-like ways. Thus, it is not clear if very significant deviations from human-like (temporal) performance are likely to be useful.

5.4. Stabilization

Retargeting of motion capture requires determining the coordinate frame of the skull. The motion of this frame is removed, and the remaining motion of the face determines the facial expression. The rigid coordinate frame of the skull is not easily determined, however, and if it is poorly estimated subsequent analysis may conflated head motion with expression change. The issue is that people cannot naturally produce expressions without simultaneously moving the head.

One approach to this problem is to attempt to find at least...
three relatively stationary points on the face, and estimate the rigid transform from these – typical candidates are the corners of the eyes and the nose tip. However, some people slightly move these points (relative to the skull) while making extreme expressions. Another solution is to identify the head motion using a rigid hat. However vigorous movement or particular expressions (such as raising the eyebrows strongly) may cause the hat to move slightly. Facial expressions can be very subtle (consider the geometric difference between a face expressing the two emotions ‘calm’ and ‘contempt’).

[BB14] introduced an approach to this important problem. It first deform a generic skull model (including a nose) to fit manually specified landmarks on a neutral pose of the actor. Then, the rigid position of the skull relative to a new scan of the face surface is determined by optimizing a cost involving the expected distance (thickness) between the skin and the skull and a second cost involving the nose length. The results are validated by comparison of the stabilized upper teeth to those in reference images. An earlier approach [XCK04, CXH03] treats the problem of separating rigid motion from deformation as a matrix factorization problem. That approach requires that the face position is described by a set of 3D tracking markers, i.e. the correspondence problem is solved, and the tracked points are a discrete set of markers rather than dense motion capture.

5.5. Partially-automated animation
In practice, performance-driven animation is rarely used without subsequent manual adjustment. One reason for this is lack of fidelity or errors in the motion capture process. For example, marker-based systems typically place markers around the outside of the mouth are thus not able to track the inner contour of the lips ( [BGY∗13] is a recent exception). Similarly, most motion capture systems do not track the eyes or eyelids.

There is another important reason for editing performance-driven animation: changes in the acting may be required. This may be because a performance that is automatically transferred to a different (e.g. non-human) character may not convey the intended emotion. As well, a movie director can request changes in the performance. For these reasons, a viable performance-capture system must allow for subsequent manual editing by artists. This is a major reason why existing performance capture approaches use a blendshape representation.

Subsequent editing of motion capture presents a further problem: motion capture produces weight curves with a key at every frame. This is too “dense” for artists to easily edit. [SSK∗11, LA09] introduced an optimal curve simplification technique using dynamic programming. With a GPU implementation, it can produce roughly an 80% reduction in sample density with little or no visible difference in the resulting curve.

5.6. Direct manipulation
Blendshapes have traditionally been animated with keyframe animation or by motion capture. Although inverse kinematics approaches to posing human figures have been used in animation for several decades, analogous inverse or direct manipulation approaches for posing faces and setting keyframes have appeared only recently. In these approaches, rather than editing the underlying parameters (as in forward kinematics, and keyframe animation), the artist directly moves points on the face surface and the software must solve for the underlying weights or parameters that best reproduce that expression or motion.

The evident challenge for direct manipulation of faces is that it can be a very under-constrained inverse problem – similar to inverse kinematics, but more so. In moving the hand of the character using inverse kinematics, for example, the animator specifies a goal point (3 degrees of freedom), and animation system must solve for on the order of 10 degrees of freedom representing the joint angles from the hand through the shoulder. In a professional blendshape model, the analogous number of unknown weights can be 100 or more. Solving the inverse problem for direct manipulation blendshapes then means that we find a discrete function (i.e., a vector ∆w) that satisfies the constraint given by a pin-and-drag manipulation [YN03] of a 3D face model. The resultant weights are then (usually automatically) interpolated to make a whole animation. The central issue here is the choice of a strong and appropriate prior for regularizing the inverse problem.

It is important to note that professional animation requires providing both direct manipulation and access to the underlying parameters (sliders). Intuitively, this is because some edits are simply harder to accomplish using direct manipulation. In fact it is easy to argue on mathematical grounds that slider manipulation is necessarily more efficient for some edits, whereas the converse is also true – direct manipulation is necessarily more efficient for other edits. Briefly, this is because of the spreading effect of a multiplication by a non-identity matrix [LA10]. In direct manipulation the blendshape weights are in a pseudoinverse relationship to the manipulated points, and columns of the pseudoinverse tend to have a number of non-zero values.

5.6.1. Direct manipulation of PCA models
The underconstrained direct manipulation inverse problem was first solved by several approaches that use an underlying PCA representation. [ZLG∗06] develop a hierarchical segmented PCA model. User-directed movement of a particular point on the face is propagated to the rest of the face by projecting the altered point vector into the PCA subspace.
and iterating this procedure over the remainder of the hierarchy. [MA07] learn a PCA subspace of facial poses. This is used to bypass computation of a majority of face points, by “PCA imputation” wherein a subset of points is computed and fit and the same linear combination is used to estimate the locations of the remaining points. [LD08] use a local, hierarchical PCA face model; facial editing is performed with a constrained version of weight propagation [ZLG*06]. This provides local control while also allowing natural cross-region correlations. [LCXS09] develop direct dragging and stroke-based expression editing on a PCA model obtained from motion capture data, and include a statistical prior on the space of poses.

These PCA approaches are good solutions if the model will be manipulated exclusively with direct manipulation, and this is the most appropriate choice for novice users. Since professional animation also requires access to the underlying sliders however, this in turn necessitates the use of an underlying blendshape representation rather than PCA due to the lack of interpretability of the PCA basis (section 7.7). While it is easy to interconvert between PCA and blendshape models (section 7.8), doing so requires having a blendshape model.

5.6.2. Direct manipulation of blendshapes

[ZSCS04] included a direct manipulation algorithm in their facial capture system. It used a basis of selected frames from a captured performance, and allows direct face editing using local and adaptive radial basis blends of basis shapes. They introduced an interesting regularization for the direct manipulation inverse problem, in which the basis meshes most similar to the desired constraints are weighted more heavily. This is an effective approach to extending the span of a model with a limited number of shapes (see Figure 6 (d),(e)) in [ZSCS04], though with a more extensive model this property might be considered undesirable.

The inverse problem can be avoided by using a fully constrained approach, exactly as would be used for performance driven animation. In this approach the artist interacts with manipulators that serve the same role as motion capture markers. The manipulators cover the face and are moved one at a time, with the others remaining stationary. The first published approach to direct manipulation of blendshape models [JTDP03] used this approach.

While constraining the face with a full set of manipulators avoids the inverse problem, it can also increase the required number of edits since no part of the face is free to move without intervention from the artist. Formulating direct manipulation as an underconstrained inverse problem allows many parts of the face to move during each edit, but requires a sensible regularization to make this useful (the previous fully constrained version of the problem can be recovered as a special case by adding sufficient constraints). [LA10] started with the principle that moving a particular part of the face should cause the remainder of the face to change as little as possible – a principle of “least surprise”. To embody this in an algorithm, they observe that the blendshape model itself is designed as a semantic parameterization, that is, the targets are sculpted so that facial expressions can be described by the combination of n sliders, each with approximately equal effect on the facial expression. This is in contrast to PCA, where the subsequent coefficients by definition have smaller influence. Thus the change in facial expression is to a first approximation represented by the change in weights, as demonstrated in Figure 1. In this figure Euclidean distance on the control vertices indicates that the full smile and open-mouth expressions are most similar, but the distance between the blendshape weight vectors correctly indicates that the smile is semantically and perceptually more similar to the half-smile.

[SILN11] presents a direct manipulation system suitable for use in animation production, including treatment of combination blendshapes and non-blendshape deformers. They add an improved regularization term that better handles the common case where the artist repeatedly moves a single slider over the same range of values in order to understand its effect. The nonlinear components of their production-quality rig are handled with a combination of nonparametric regression (for the jaw) and a derivative free nonlinear optimizer. [ATL12] describes an extension of the direct manipulation approach [LA10], which allows more efficient edits using a simple prior learned from facial motion capture. This system also allows the artist to select between three different modes at any time during editing: sliders, regular, and learned direct manipulation (see section 7.8). [COL15] describe an approach in which the artist designs direct manipulation manipulators by sketching. [NVW*13] show direct manipulation of an automatically created local linear model. This work is discussed in section 4.2.
5.7. Further interaction techniques

[PHL*98] proposes a painterly interface for creating facial expressions. The interface has three components: a canvas for designing a facial expression, a brush interface that allows the user to select the intensity and decay of the strokes, and a palette where the colors are replaced by facial expressions. When a stroke is applied to the facial canvas, weights from the selected facial expression are transferred to the facial palette and selected to design more complex expressions. While direct manipulation offers advantages over the traditional slider editing, a more fluid or “sketch based” interface [MAO*11] might be preferable for both novice users and for previsualization of professional animation. Development of sketch-based interfaces that incorporate an underlying blendshape basis is an open problem.

5.8. Summary

Methods for automated tracking, expression cloning, and interacting with blendshape models are well developed. Open areas may include expression cloning methods that consider differing characteristics of the target model, e.g., those resulting from considerable differences of anatomy or size. Another open area may be the development of interfaces (e.g., sketch-based interfaces) for faster and more fluid manual animation.

6. Facial Animation as an Interpolation Problem

Blendshapes are perhaps the simplest approach to facial animation imaginable, and limitations of the linear model are evident. In this section we discuss blendshapes in abstract as a problem of interpolation, and consider whether a better approach may be possible.

6.1. Blendshapes as a high dimensional interpolation problem

In abstract, facial animation is an interpolation problem of the form

\[ f : \mathbb{R}^n \rightarrow \mathbb{R}^{3p} \]

that maps a set of \( n \) animation control parameters (such as \( n \approx 100 \) for blendshape sliders) to the \( 3p \) values, where \( p \) is the number of control vertices of the 3D face model.

6.2. Linear interpolation

The linear nature of blendshapes affects the animation in some cases. In the interpolation from one target to another, two weights change in a convex combination, and the movement of each changing vertex is necessarily along a line. Animators are aware of this limitation [Tay] and have sometimes compensated for it by adding additional sculpted shapes that are interpolated on the animation timeline. If the two weights are not in an affine (sum-to-one) combination, the movement is constrained to a plane, etc. More generally, the blendshape scheme constrains movement to a \( n \) dimensional subspace of the \( 3m \)-dimensional ambient space.

6.3. Scattered interpolation

A scattered interpolation scheme might seem an ideal solution to the problem of interpolating a number of targets in a high dimensional space, since the sculpted faces could be placed at arbitrary (scattered) desired locations in the parameter space \( \mathbf{w} \) (Figure 11). In a radial basis function (RBF) approach the kernel could be chosen as the Green’s function of a differential operator, resulting in smooth interpolation of the data. This formulation would also separate the number of targets from the dimensionality of the space.

Unfortunately, high-dimensional interpolation is known to be intrinsically difficult [Ca98, Gar]. The Green’s function corresponding to the differential operator family \( \nabla^{2s} \) is defined as [Duc76, LPA10]

\[ R(x) \propto \begin{cases} \left\| x \right\|^{2s-n} \log |x| & \text{if } 2s-n \text{ is an even integer}, \\ \left\| x \right\|^{2s-n} & \text{otherwise} \end{cases} \]

for smoothness order \( s \) and space dimension \( n \).

This requires a condition \( 2s > n \) in order to avoid having a singularity at the origin. A potentially more difficult problem is the curse of dimensionality [HTF09], which suggests that the number of data samples required for interpolation in \( n \) dimensions is exponential in \( n \), unless the interpolation scheme can identify that the data lives on a lower-dimensional manifold or makes other simplifying assumptions.

Thus, we have the open problem of interpolating in a high (e.g., \( n = 100 \)) dimensional space. One possibility would be to dramatically increase the order of smoothness \( s \), to \( s > n/2 \approx 50 \). While this has not been explored, it can be noted that in other applications in computer graphics \( \mathcal{C}^2 \) smoothness has often proven sufficient, and at present we have no reason to believe that the motion of the face between expressions is extremely smooth.

6.4. Blendshapes as a tangent space

Equation 4 resembles a vector-valued Taylor series expansion about the neutral face, i.e.,

\[ f(w) = f(0) + \frac{\partial f}{\partial w} \cdot w \]

with \( f(0) \equiv \mathbf{b}_0 \) and the Jacobian \( \left[ \frac{\partial f}{\partial w} \right] \equiv \mathbf{B} \). In abstract geometric terms, we might consider blendshapes to be the tangent space (about the neutral face) of the \( n \)-dimensional face “manifold” embedded in a \( m \)-dimensional ambient space.
Figure 11: Blendshape schemes require that targets are placed at constrained locations, i.e. the vertices of a “weight hypercube” (Figures 5, 7). It would be preferable to allow targets to be placed anywhere in face space, allowing the sculpting effort to be directed specifically where it is needed.

As we move from one point to another along this (for example) 100-dimensional tangent space, the location in the $m = 30000$ dimensional ambient space also changes.

This comparison to a Taylor series suggests limitations of the blendshape approach, and one wonders whether an alternative approach is possible. The blendshape approach requires the artist to sculpt $n$ shapes at all the locations in weight space $w_k = \delta_{i,k}$ for $k = 1 \ldots n$ (the vertices of the hypercube connected by an edge to the neutral shape, (Figure 5), i.e. the “one-ring” of the neutral). It is not possible for the artist to specify shapes at an arbitrary location such as $w = 0.3, 0.7, 0.1, \cdots$ (Figure 11). If the facial model is incorrect at an arbitrary location, current systems require the artist to modify a number of targets so that their weighted sum reduces the desired correction, while simultaneously not disturbing other face poses. This is a time-consuming iterative refinement procedure.

[SSK*12] described a hybrid approach in which a basic blendshape model is augmented with additional nonlinear corrections. The corrections are interpolated by a radial basis function scheme inspired by weighted pose space deformation [KM04], with the underlying blendshape weights defining the pose space. This approach allows shapes to be placed as needed at any pose of the model (Figure 11) and the interpolation is smooth and free of artifacts such as the quadratic ramp-up that occurs with combination shapes (section 3.3).

6.5. Summary

Interpolation in high dimensions is an open problem and an active subject of research in machine learning. Current approaches include additive models and (more generally) smoothing spline ANOVA models [Wah09, Gu13], and approaches that make use of the manifold assumption. Interestingly, [KM04] can be seen as partially addressing the curse of dimensionality inherent in high dimensional interpolation, by breaking the global interpolation problem into a collection of softly coupled local problems.

7. The Blendshape Parameterization

Despite the simplicity of the blendshape representation, there are a number of associated issues. The distinction between blendshapes and other linear models such as PCA is at the heart of the definition of blendshapes – indeed, otherwise there would be no need for a separate term. These issues will be surveyed in this section.

7.1. Lack of orthogonality

Figure 12: Mutual coherence plot for the 46-target blendshape model shown in Figure 10 and other figures. The $i, j$ entry is the covariance between the $i$-th and $j$-th blendshape targets, i.e. $\frac{b_i^T b_j}{\|b_i\| \|b_j\|}$.

The major distinguishing characteristic of blendshapes relative to the more common principal component representation is that the shapes are not orthogonal (Figure 12). This has the advantage of interpretability (section 7.6). It has the disadvantage that the parameters are correlated, and so adjusting a parameter can degrade the effects obtained with previous edits. [LMDN05] addressed this problem with a user-interface technique in which the artist can “pin” particular points representing desirable aspects of the current facial expression, and subsequent edits occur in the approximate null-space of these constraints.

7.2. Blendshape models are not unique

Given a particular blendshape model, there are an infinite number of other blendshape models that can produce the same range of animation. Intuitively, this is similar to the fact
that an infinite number of vector pairs span the plane, and
given two such vectors (analogous to a particular “model”),
another pair can be constructed as weighted combinations of
the original vectors - for example the sum and difference of
the original pair is one such basis. Given a particular blend-
shape model \( B \), an arbitrary non-singular \( n \times n \) matrix \( R \) and
its inverse can be inserted between the \( B \) and the weights
without changing anything:

\[
f = B \left( RR^{-1}\right) w
\]

Then \( BR \) is a new blendshape basis with corresponding
weights \( R^{-1}w \) that produces the same range of motion as
\( B \).

7.3. Equivalence of whole-face and delta blendshape
formulations

Proponents of various blendshape approaches are outspoken
in industry forums regarding the proposed advantages of
each particular approach. While working in the entertain-
ment industry, one of the authors heard emphatic claims that
the delta form is the most powerful form of blendshape,
or alternately that using targets modeled after the FACS
poses [SG06, ER97] is the only approach that produces all
and only the full set of valid face shapes. In fact it is simple
to show that, while these techniques have their respective
advantages, they are equivalent in expressive power and the
desired range of expressions does not uniquely specify a
blendshape model.

The delta formulation equation (4) and the whole-face form
equation (2) can be seen to be equivalent (in the terms of the
range of shapes produced) by rewriting equation (1) as

\[
f = \sum_{k=0}^{n} w_k b_k
\]

\[
= w_0 b_0 + \sum_{k=1}^{n} w_k b_k
\]

\[
= w_0 b_0 + \sum_{k=1}^{n} w_k b_k - \sum_{k=1}^{n} w_k b_0 + \sum_{k=1}^{n} w_k b_0
\]

\[
= \left( \sum_{k=0}^{n} w_k \right) b_0 + \sum_{k=1}^{n} w_k (b_k - b_0)
\]

(6)

If the whole-face weights are convex (as is generally the
case) this exactly recovers the delta-face formulation (3).

It is intuitive to think of local blendshapes as having more
power for a given number of targets. For example, if there are
\( n_1 \) shapes for the mouth and lower face, \( n_2 \) for the right eye
and brow, and \( n_3 \) for the left eye and brow, then we may be
tempted to consider that the resulting system would require
\( n_1 \cdot n_2 \cdot n_3 \) whole-face shapes to have equivalent power. In
fact this is incorrect, as suggested by equation (6) above. As
an analogy, consider a pixel (sample) basis and a Fourier ba-
sis. The former is maximally local, yet spans the same space
as the latter.

As an example, consider a blendshape model that has these
targets: left-eye-closed, right-eye-closed (as well as the neu-
tral shape). In the delta scheme, creating a model with both
eyes closed requires corresponding weights \((1,1)\). In the
whole-face scheme, setting the weights to \((1,1)\) would cause
the head to scale, whereas setting them to \((0.5,0.5)\) will give
a the result of two half-closed eyes. However if we no-
tate the delta blendshapes as \( b_1, b_2 \), and the corresponding
whole-face targets as \( B_1 = b_1 + n, B_2 = b_2 + n \), simple alge-
bra gives the result that the desired closed-eye expression in
delta form, \( b_1 + b_2 + n \), is equivalent to \( B_1 + B_2 - n \). Note
that this is not a convex weight combination.

7.4. Global versus local control

In general, both global and local specification of shape de-
formation may be desirable. Global specification is desirable
when the modeler is given a picture or sculpted maquette of
a complete head that they must match with a computer model.
Modeling a set of heads with various facial expressions is a
more natural task than modeling the corresponding “delta”
shapes such as the displacements governing eyebrow move-
ment. Global specification is also used in some animation
scenarios, such as the time-dependent blendshape modeling
approach mentioned in section 2.

On the other hand, many animation tasks are more easily ap-
proached if local control is available. For example, increasing
the width of the mouth is more easily accomplished if only
one or a few blend shapes affect the mouth region than in
the situation where every basis vector affects all regions of
the face including the mouth. While producing the de-
sired effect should be possible in an equivalent system of
non-localized blendshapes (equation (6)), the global effect of
each blendshape combined with their interaction with other
shapes (see section 7.1) results in a tedious trial and error
process for the artist. Fortunately, equation (6) points out that
converting between whole-shape and delta formulations is a
simple matter. Because of this equivalence and the simplic-
ity of converting between the whole-face and delta formul-
ations, it is not necessary to restrict oneself to the choice of
one representation over the other – the user interface can
allow the artist to select between the whole-face and delta
forms according to the particular task.

As noted above, local control can be obtained with the delta
blendshape formulation if the changes in the target faces are
restricted to small areas. This may be difficult to obtain in
some common modeling methodologies, however, as when
the target faces are digitized from physical models. We also
noted that local control can be guaranteed by segmenting
the face into separate regions each of which has an inde-
pendent set of blend shapes [Kle89, JTD03]. Unfortunately
the ideal segmentation may be difficult to choose in ad-
Figure 13: The space of valid face shapes, represented abstractly as the curved shaded region, is approximated as a convex combination of a number of blendshapes lying on the boundary of the region (black circles). Some regions of the space are not reachable with these blendshapes. This can only be addressed by sculpting blendshapes that lie outside of the valid face space. This is an unnatural task for the modeller.

7.5. Convex combination of shapes

Whole-face blendshape interpolation can be restricted to convex combinations by enforcing the following constraints on the weights

$$\sum_{k=1}^{n} w_k = 1, \quad w_k \geq 0, \quad \text{for all } k.$$  \hspace{1cm} (7)

These constraints guarantee that the blendshape model lies within the convex hull of the blendshapes. This is a reasonable first assumption, but it is desirable to relax it. By analogy with the convex hull containing a two-dimensional face space (Figure 13), it is likely that targets sufficient to span a broad range of facial expressions must themselves lie outside the valid range of expressions. Because it is somewhat unnatural to ask an artist to sculpt targets that are slightly beyond the range of plausible expressions, it is often desirable to slightly relax the constraint in equation (7).

Constraining the weights to sum-to-one results in an inconvenient parameterization in which the model has \(n\) user parameters for \(n - 1\) degrees of freedom, and any weight can be expressed as a linear combination of the other weights. In practice it means that the blending weights cannot be modified independently (e.g. using sliders) without violating the constraint. One solution is to normalize the weights after each modification. From the user interface point of view, this has the undesirable consequence that changing a particular weight will cause other weights that were not explicitly altered to change as well. Animators are not novice computer users, however, and can learn to anticipate this behavior.

7.6. Semantic parameterization

The blendshape basis has meaning by construction: blendshape targets have simple and definable functions such as raise-right-eyebrow. This allows the effect of particular targets to be predicted and remembered, thereby reducing trial-and-error exploration during animation.

Recent literature in several fields explores the idea that sparse, positive, non-orthogonal, and redundant bases are better able to encode aspects of the meaning of a signal. Examples of this literature include non-negative matrix factorization [LS99], sparse coding for image processing [Ela10], and modeling of biological information processing [OF96]. We note that blendshapes share the qualities of being a non-orthogonal and sparse representation. The blendshape weights are (usually) positive, but the basis is not redundant. A well-constructed blendshape model produces reasonable facial expressions when a few weights (up to five or so) are non-zero, but the models fail when many weights are active (Figure 14). Figure 15 compares the sparsity of the blendshape encoding to a PCA encoding. The blendshape weights are usually either large or zero, and relatively few weights are active at any point. The PCA representation of the animation has a large number of very small weights. These dense
and small weights would be difficult (and laborious) to specify using keyframe animation.

7.7. PCA is not interpretable

While the first few basis vectors discovered by PCA are often interpretable (for example, the first eigenvector typically reflects the jaw-opening motion), the remaining basis vectors are notoriously difficult to interpret. In this section we explain this lack of interpretability in three ways:

- by intuitive argument: a target such as raise-right-mouth-corner is obviously not orthogonal to jaw-open (the jaw-open motion pulls the mouth corner down slightly).
- by demonstration: Figure 16 shows several eigenvectors from a professionally created facial animation, (visualized with the mean added as face meshes). The deformations are global and hard to understand and use.

Figure 16: PCA basis vectors are difficult to interpret and remember. These are the 9th and 10th eigenvectors from a professionally produced facial animation.

Figure 17: PCA is a weak “model” of data. From left to right: a synthetic data set, the PCA coefficients of this data, the rotated PCA coefficients, and random points having the same covariance as the data. While the two eigenvectors and corresponding eigenvalues capture the spread of the data, all the structure ends up in the coefficients. In this two dimensional example the coefficients $c = U^T f$ are simply a rotation of the original data points $f$, since $U$ is orthogonal.
• By mathematical arguments:

1. (An informal variant of the Courant nodal theorem for eigenfunctions of the Laplacian): The second constructed eigenvector is orthogonal to first eigenvector. Consider a hypothetical case where the first eigenvector is everywhere non-negative. In order to be orthogonal, the second eigenvector must have both positive and negative regions over the support of the positive part of the first eigenvector. Thus we see that each eigenvector will tend to have more oscillations than the previous. While the nodal theorem applies to the eigenvectors of the Laplacian, the Laplacian functions as an inverse covariance [LRZ14], and the eigenvectors of a matrix are the same as those of its inverse. Note that this argument follows from the orthogonality of the basis, and thus applies equally to PCA variants such as weighted PCA.

2. The eigenvectors are linear combinations of all the variables (this is a motivation for sparse PCA schemes). PCA is the orthogonal basis that minimizes the squared reconstruction error. By the “grouping effect” of least squares [ZH05], if a group of correlated variables contributes to an eigenvector, their contribution tends to be distributed evenly across all variables.

PCA is also quite weak as a means of characterizing or modeling data (Figure 17). The data covariance used in PCA uniquely specifies a Gaussian distribution, but non-Gaussian data may also have the same covariance. PCA is thus a viable “model” only if the data is jointly Gaussian, which is not true for either facial proportions ([LMAR14]) or facial movement. Figure 18 shows scatterplots of several coefficients of the PCA representation of a professionally created animation. The clearly visible structures in this figure illustrate that facial movement is highly non-Gaussian: since the PCA coefficients are a linear function of the data (after removing the mean), and linear transforms preserve Gaussian distribution (indeed transformed non-Gaussian data tends to be more Gaussian than the original), these scatterplots would be Gaussian if the data were Gaussian.

PCA is a particular example of unsupervised learning. Other unsupervised learning approaches have also been applied to facial animation. [CFP03] use Independent Component Analysis (ICA), which tries to extract linear components that are statistically independent, a stronger property than the uncorrelated components used by PCA. They show that the extracted components can be categorized in broad motion groups such as speech, emotions, and eyelids. The components can then be used for coarse motion editing such as exaggeration.

Figure 18: Scatterplot of the 1st vs. 3rd PCA coefficients (top) and 2nd vs. 3rd PCA coefficients (bottom) of the professionally-created 405-frame facial animation used in Figure 15. The plots show clear non-Gaussian structure. Note that many points are coincident and overlaid in the upper figure.

Figure 19: Probability that a sample from a unit variance Gaussian lies outside the unit hypersphere for various dimensions.
7.8. Conversion between blendshape and PCA representations

A blendshape representation can be equated to a PCA model that spans the same space:

\[ \mathbf{Bw} + \mathbf{f}_0 = \mathbf{Uc} + \mathbf{e}_0 \]  

(8)

where \( \mathbf{U} \) and \( \mathbf{e} \) are the PCA eigenvectors and coefficients, and \( \mathbf{f}_0 \) and \( \mathbf{e}_0 \) are the neutral face and mean face respectively. The weights can be interconverted as

\[
w = (\mathbf{B}^T \mathbf{B})^{-1} \mathbf{B}^T (\mathbf{Uc} + \mathbf{e}_0 - \mathbf{f}_0) \\
c = \mathbf{U}^T (\mathbf{Bw} + \mathbf{f}_0 - \mathbf{e}_0)
\]

Note that the matrices here (e.g. \( \mathbf{(B^T B)^{-1} B^T U} \)) can be precomputed and are of size \( n \times n \). The vectors \( \mathbf{(B^T B)^{-1} B^T (e_0 - f_0)} \) can also be precomputed. Thus converting from weights to coefficients or vice versa is a simple affine transform that can easily be performed at interactive rates on current machines. A blendshape software system can thus internally convert operations into a PCA representation if this is advantageous.

7.9. Probability of a blendshape expression

Various applications require or can benefit from knowing the “probability” of a facial expression. The Gaussian density leads to simple MAP (maximum a posteriori) computation, so this approach is widely used in many applications. The probability and norm can be used to identify outliers in the “probability” of a facial expression. The Gaussian density with these variances can be used to assign a probability and norm can be used to identify outliers in the “probability” of a facial expression.

The correspondence of blendshapes and PCA representations (equation 8) gives a simple means to assign a probability to a blendshape expression. The expectation of the square of an individual PCA coefficient is the corresponding eigenvalue:

\[
E[\mathbf{c}_i^2] = E[\mathbf{u}_i^T \mathbf{ff}^T \mathbf{u}_i] \\
= \mathbf{u}_i^T E[\mathbf{ff}^T] \mathbf{u}_i = \mathbf{u}_i^T \mathbf{C} \mathbf{u}_i \\
= \mathbf{u}_i^T \lambda_i \mathbf{u}_i \\
= \lambda_i \text{} \because \text{because } ||\mathbf{u}_i|| = 1
\]

where \( \mathbf{f} \) is a vector representing the face (or other data) with the data mean removed, \( \mathbf{u}_i \) is a particular eigenvector and \( \lambda_i \) is the corresponding eigenvalue.

Since the eigenvalues are variances, the multivariate normal density with these variances can be used to assign a probability to a facial expression:

\[
P(\mathbf{c}) = \exp \left( -\frac{1}{2} \sum \frac{c_i^2}{\lambda_i} \right) = \exp \left( -\frac{1}{2} \mathbf{c}^T \mathbf{A}^{-1} \mathbf{c} \right)
\]

This also generates a “face norm” \( ||\mathbf{f}||_G \):

\[
\mathbf{c}^T \mathbf{A}^{-1} \mathbf{c} = (\mathbf{f}^T \mathbf{U})(\mathbf{U}^T \mathbf{C}^{-1} \mathbf{U})(\mathbf{U}^T \mathbf{f}) = \mathbf{f}^T \mathbf{C}^{-1} \mathbf{f} = ||\mathbf{f}||_G^2
\]

The form \( \mathbf{f}^T \mathbf{C}^{-1} \mathbf{f} \) is the multidimensional counterpart of the argument \( f^2/2\sigma^2 \) that appears in the one-dimensional Gaussian \( \exp(-f^2/2\sigma^2) \).

There is an important but rarely acknowledged issue with assigning a Gaussian probability to face models however [LMAR14]: MAP seeks the mode of the posterior Gaussian. In high dimensions the Gaussian is a heavy tailed distribution, and the mode is a highly atypical point – the interior of the density has almost no volume, and (contrary to some published statements) typical faces drawn from this density will not lie near the mean (Figure 19).

7.10. Summary

Although the blendshape idea is extremely simple, careful consideration reveals fundamental issues including high dimensional interpolation (section 6), semantic parameterization, and sparse coding. In fact blendshapes provide an interesting “workshop” for discussing general issues of representation and parameterization. The contrast between blendshape representations and principal component analysis is particularly interesting.

8. Generalizations and Future Directions

We conclude by briefly mentioning two techniques that accomplish nonlinear blending of target shapes. While these are outside of the industry definition of blendshapes, they point the way toward more powerful techniques.

Rather than forming a linear combination of the positions of various target shapes, [SZGP05] blend deformation gradients. Specifically, they split the Jacobian into rotation and symmetric factors using polar decomposition and then do...
linear interpolation in the rotation Lie algebra using the exponential map. The symmetric factor is directly linearly interpolated (symmetric matrices are not a group, but linear interpolation of symmetric matrices preserves the property). This approach might be considered as a nonlinear generalization of the blendshapes.

[MBF+12] interprets the original target meshes as a mass spring model and linearly blends edge lengths rather than geometry. This simple approach is able to produce reasonable rotational motion (Figure 20) as well as contact and collision effects.

8.1. Summary

From the viewpoint of current graphics research, the blendshape approach is primitive, and improvements or a successor would be welcome. A direct successor to this approach would need to have several characteristics:

1. The ability to construct the model by directly sculpting or scanning facial expressions,
2. Artists should be able to understand and edit the model’s underlying parameters
3. The computation should be relatively lightweight, allowing real-time playback of interactive edits

The algorithms [SZGP05, MBF+12] satisfy at least the first two requirements and suggest the way forward.

9. Conclusion

“Blendshapes” are at present the leading approach to realistic facial animation. While most algorithms in graphics industry software and practice can be traced back to original research publications, blendshapes are unusual in that both the original idea and some recent developments such as combination shapes [OSi07] originated outside of academic forums. Despite its simplicity and popularity, the technique has both unresolved limitations and associated open problems. Facial blendshapes are also an attractive “workshop” for exploring issues of representation and parameterization.

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The relevant literature on this topic is large and difficult to fully survey. We regret omissions.

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